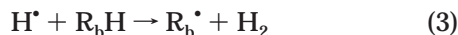
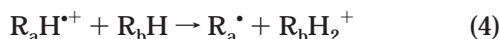




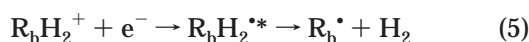
Radical pairs are generated by hydrogen atom ejection following the recombination reaction:<sup>3,7</sup>



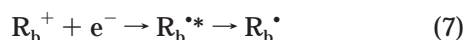
An alternative mechanism, which was given in the overview but not thought to be significant, is that of proton or hole transfer between precursor radical cations and neighboring alkyl chains:



A large body of information exists implicating such charge-transfer reactions as radical migration processes.<sup>9,10</sup> The cation produced in reaction 4 is liable to electron capture, either before ejection of a hydrogen molecule



or after ejection of a hydrogen molecule



The net result is similar to that predicted in the H atom ejection model used in the generator of our previous HDPE study, in that partner radicals are produced predominantly between carbon atoms of adjacent chains. However, unlike hydrogen atom abstraction by ejected H atoms, proton transfer, from cation radicals in the ionic mechanism of partner radical formation, is bound to be site selective, because the proton affinity of neighboring acceptor C–H bonds is expected to decrease in the order of tertiary C > secondary C > primary C.<sup>9</sup> Site selectivity of this nature would affect preferred partner ratios and radical-pair distance distribution functions, being more apparent in PP than in PE, because the pendant methyl groups, which are primary carbon atoms, ensure that every other carbon of the PP main-chain backbone is tertiary, whereas in PE secondary main-chain carbons predominate almost exclusively.

To include the mechanisms of proton transfer into the radical-pair generator would necessitate intensifying what is already a lengthy and complex program, and employing estimates of probabilities for the various reaction pathways which are as yet not accurately defined for PP. Hence, in this paper, as in the previous work on amorphous HDPE,<sup>1</sup> a first approximation for radical-pair data was obtained using the simple H atom ejection model. It should be remembered that this simple radical-pair generator amply reproduced the experimental results of Dubinskii et al.<sup>5</sup> in the modeling of amorphous HDPE. Also, at low numbers of cross-links per number-average molecule, the number of “gel-effective” cross-links determined in LLDPE using the same radical-pair generator<sup>2</sup> proved to be in good agreement with the total numbers of cross-links determined by rheology.<sup>3,4</sup> Some of the inaccuracies incurred by not invoking proton transfer may have been accommodated for in the cone angle of hydrogen atom ejection ( $\phi = 15^\circ$ ) used in the simple generator. Nevertheless, the reproduction of experimental results indicates that proton transfer is of minor importance in radical-pair

**Table 1. Probabilities of Partner-Radical ( $r_p$ ) Formation in Amorphous PP (Head to Tail,  $\rho = 0.90 \times 10^3 \text{ kg m}^{-3}$ ):<sup>a</sup> i-PP**

initiating radical	a-type partners	b-type partners	c-type partners
a-type radical	0.3066	0.1744	0.5189
b-type radical	0.3150	0.1584	0.5266
c-type radical	0.3004	0.1614	0.5381
mean	0.3073	0.1647	0.5279

<sup>a</sup> Mean  $\equiv$  completely random a-, b-, c-type radical initiation.

**Table 2. Probabilities of Partner-Radical ( $r_p$ ) Formation in Amorphous PP (Head to Tail,  $\rho = 0.90 \times 10^3 \text{ kg m}^{-3}$ ):<sup>a</sup> s-PP**

initiating radical	a-type partners	b-type partners	c-type partners
a-type radical	0.3305	0.1409	0.5286
b-type radical	0.3033	0.1623	0.5344
c-type radical	0.3066	0.1478	0.5456
mean	0.3135	0.1503	0.5362

<sup>a</sup> Mean  $\equiv$  completely random a-, b-, c-type radical initiation.

**Table 3. Probabilities of Partner-Radical ( $r_p$ ) Formation in Amorphous PP (Head to Tail,  $\rho = 0.90 \times 10^3 \text{ kg m}^{-3}$ ):<sup>a</sup> a-PP**

initiating radical	a-type partners	b-type partners	c-type partners
a-type radical	0.2976	0.1464	0.5560
b-type radical	0.2840	0.1591	0.5569
c-type radical	0.3065	0.1559	0.5376
mean	0.2960	0.1538	0.5502

<sup>a</sup> Mean  $\equiv$  completely random a-, b-, c-type radical initiation.

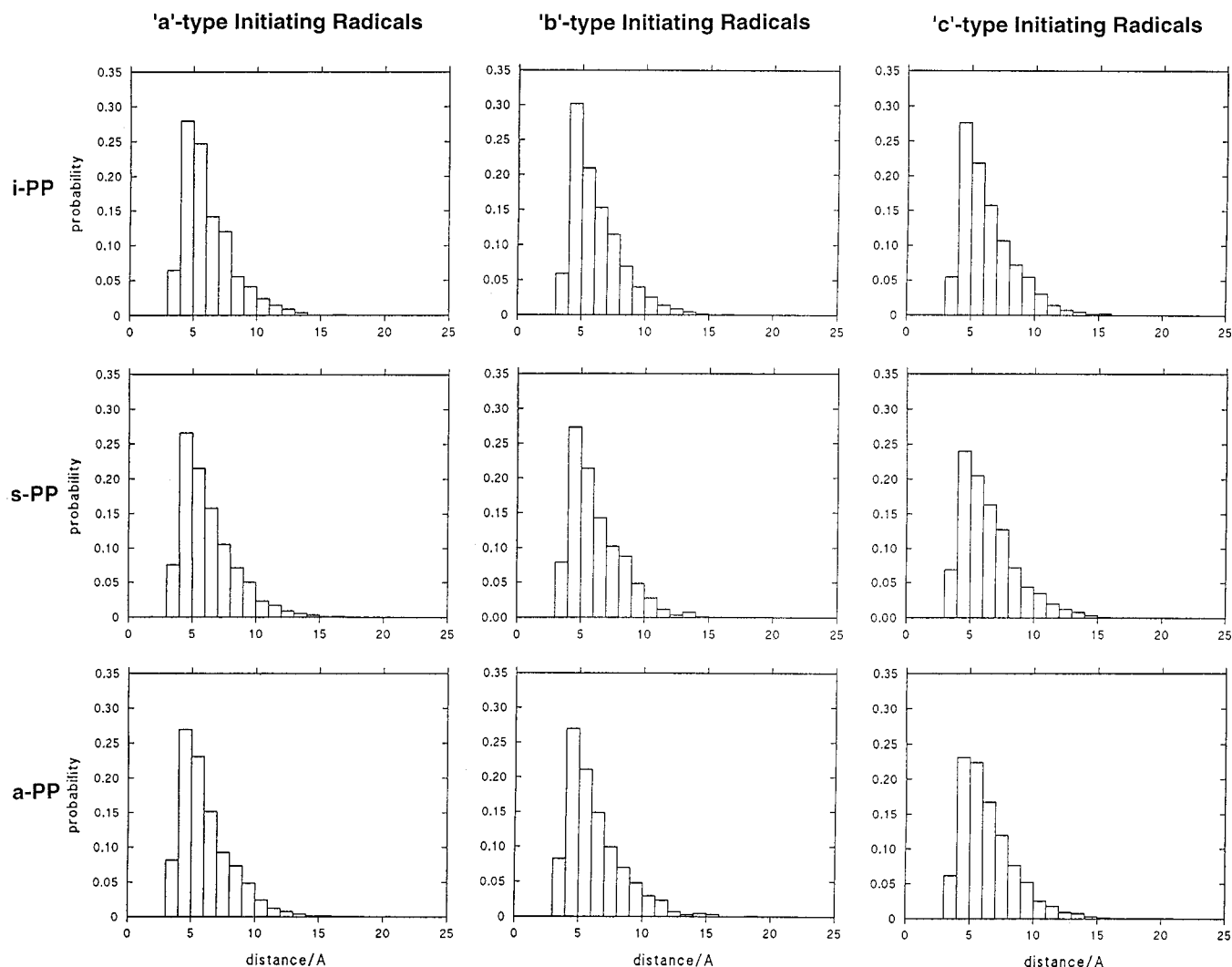
formation, at least for PE, and hence, we believe for related poly(alkenes) also.

### Computational Model

Essentially, the model is as outlined in our previous publication on HDPE,<sup>1</sup> but with modifications for PP. Hydrogen atom ejection was modeled in amorphous PP macrocells (MSI, Insight II, Version 400).<sup>11</sup> Chains consisting of 1000 propylene monomer units, with two end groups per chain, were packed into amorphous subcells at densities of  $(0.85\text{--}0.94) \times 10^3 \text{ kg m}^{-3}$ . Each unit subcell contained one chain, equilibrated for greater than 1000 molecular dynamics steps (293 K) under periodic boundary conditions. The macrocells contained 24 000 carbon atoms in 8 interlocking unit subcells. Hence, there were 72 016 atoms in total, inclusive of hydrogen atoms.

A program was written in “C” to read the Cartesian coordinates of the individual atoms in the equilibrated MSI macrocell and store the coordinates, relative to the center of the cell, in one-dimensional arrays. Radical-pair formation was considered to take place in the macrocell under static rather than dynamic conditions, because hydrogen atoms are ejected within the lifetime of a single vibration ( $\sim 10^{-13}$  s), and move at least 4 orders of magnitude faster than the polymer segmental motions ( $> 1$  ns). The minimum velocity of a hydrogen atom moving under random thermal motion is  $\sim 2 \times 10^4 \text{ Å ns}^{-1}$ . Hence, the “initiating” hot-hydrogen atoms reach neighboring chains and react with them before chain motions takes place.

The method of radical-pair generation used in this study has been well-described previously, with the following constants applied to the generator: van de Waals radii for hydrogen and carbon, 1.0 and 1.7 Å, respectively, and the cone angle of hydrogen atom ejection ( $\phi$ ) was taken to be  $15^\circ$ , being the angle which most closely reproduced experimental results in HDPE.<sup>1</sup> The distance of atomic screening from the ejection site was increased up to 40 Å. To improve accuracy of the radical-pair distribution functions, the generation off possible partner radicals was repeated 10 000 times. After 10 000



**Figure 2.** Atomistic radical-pair distance probability distribution functions for available partners in amorphous i-, s-, and a-PP ( $\rho = 0.90 \times 10^3 \text{ kg m}^{-3}$ ).

**Table 4. Statistical Availability of Hydrogen Atoms in PP**

	C <sub>a</sub> -hydrogen atoms	C <sub>b</sub> -hydrogen atoms	C <sub>c</sub> -hydrogen atoms
available H atoms	2	1	3
ratio of availability	0.3333	0.1667	0.5

iterations, the sum of the frequencies in the histogram intervals was normalized, such that the total frequency was unity with respect to radical initiation, to give the fractional number of partner radicals per initiating radical generated.

## Results and Discussion

**1. Probabilities of Radical Sites.** The probabilities of partner-radical formation, as found by our atomistic statistical model applied to i-PP, s-PP, and a-PP, are shown in Tables 1–3, respectively, for radical initiation from the a-, b-, and c-type initiating radicals. The mean probability of a-, b-, and c-type partner-radical formation, taken from all three PP tacticities combined, differ by only approximately –8.31, –6.30, and +7.62% from the numerical availability of hydrogen atoms on the respective a-, b-, and c-type carbons (Table 4). Hence, the ratio of partner-radical probabilities is generally close to the numerical availabilities of hydrogen atoms. Deviations from the numerical availabilities in Table 4 therefore, reflect screening effects. The atomistic model yields of b-type partner-radicals are only slightly less

**Table 5. Probabilities of Combined Radical Formation (Initiating Radicals plus Partner Radicals) in Amorphous PP (Head to Tail,  $\rho = 0.90 \times 10^3 \text{ kg m}^{-3}$ ):<sup>a</sup> i-PP**

initiating radical	a-type combined radicals	b-type combined radicals	c-type combined radicals
a-type radical	0.6534	0.0872	0.2595
b-type radical	0.1575	0.5792	0.2633
c-type radical	0.1502	0.0807	0.7691
mean	0.3204	0.2490	0.4306

<sup>a</sup> Mean  $\equiv$  completely random a-, b-, c-type radical initiation.

than statistically expected on the basis of availability. Hence, b-type partner radicals have the lowest probability of being formed in all three PPs, because there is only one H atom available on the b carbon.

The atomistic probabilities of combined radical ( $r_c$ ) formation, initiating radicals ( $r_i$ ) plus partner radicals ( $r_p$ ), ( $r_c = r_i + r_p$ ), are shown for i-PP, s-PP, and a-PP, in Tables 5, 6, and 7, respectively, for radical initiation from the a-, b-, and c-type initiating radicals, calculated according to the following equation:

$$p(r_c)_x = \frac{1}{2} \cdot (p(r_i)_x + p(r_p)_x) \quad (i)$$

where  $x$  is the type of radical (a-, b-, or c-type) under

**Table 6. Probabilities of Combined Radical Formation (Initiating Radicals plus Partner Radicals) in Amorphous PP (Head to Tail,  $\rho = 0.90 \times 10^3 \text{ kg m}^{-3}$ ):<sup>a</sup> s-PP**

initiating radical	a-type combined radicals	b-type combined radicals	c-type combined radicals
a-type radical	0.6653	0.0705	0.2643
b-type radical	0.1517	0.5811	0.2672
c-type radical	0.1533	0.0739	0.7728
mean	0.3234	0.2418	0.4348

<sup>a</sup> Mean  $\equiv$  completely random a-, b-, c-type radical initiation.**Table 7. Probabilities of Combined Radical Formation (Initiating Radicals plus Partner Radicals) in Amorphous PP (Head to Tail,  $\rho = 0.90 \times 10^3 \text{ kg m}^{-3}$ ):<sup>a</sup> a-PP**

initiating radical	a-type combined radicals	b-type combined radicals	c-type combined radicals
a-type radical	0.6488	0.0732	0.2780
b-type radical	0.1420	0.5795	0.2785
c-type radical	0.1533	0.0779	0.7688
mean	0.3147	0.2435	0.4418

<sup>a</sup> Mean  $\equiv$  completely random a-, b-, c-type radical initiation.**Table 8. Mean Radical-Pair Distances in Amorphous PP (Head to Tail,  $\rho = 0.90 \times 10^3 \text{ kg m}^{-3}$ ):<sup>a</sup> i-PP**

initiating radicals	$\overline{r_{i,p}}/\text{\AA}$
a-type radicals	6.1185
b-type radicals	6.1470
c-type radicals	6.2834
mean	6.1830

<sup>a</sup> Mean  $\equiv$  completely random a-, b-, c-type radical initiation.

analysis. (N.B.:  $p(r)_x = 1$  when  $r_1$  and  $r_p$  are the same type, otherwise  $p(r)_x = 0$ .)

Since b-type partners have the lowest probability of being formed (Tables 1–3), and ESR spectra observed experimentally predominantly contain b-type combined radicals,<sup>6,8</sup> then nearly all the initiating radicals must be b-type in order to produce the spectra. This is demonstrated in Tables 5–7. The above premise is in keeping with excitation energy transfer theory of PP,<sup>12</sup> where most of the exciton energy is predicted to exist in the lowest exciton level ( $K = 0$ ), corresponding to pure main-chain C–C bond excitation. Somewhat less than 9% of the exciton energy is believed to exist with nonzero  $K$  values, but even then excitation of the side bond is not localized on the methyl group. Hence, most excitons do not “see” the methyl group and scission of it from the main chain is not expected. Of the main chain hydrogen atoms, the b-carbon H atom is then most easily ejected either following ion–molecule–electron recombination or as a proton ejection.

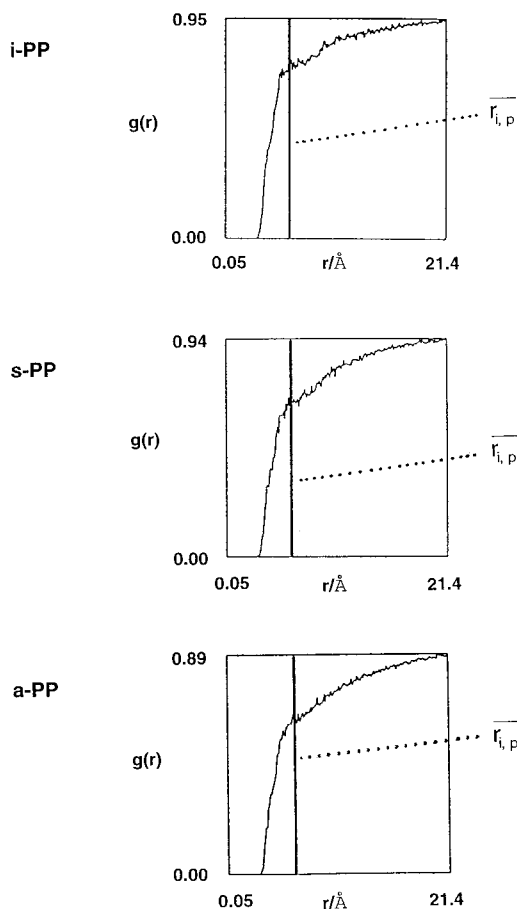
**2. Radical-Pair Distances.** The radical-pair probability-distance distribution functions, summed over all initiating radical to possible partner-radical distances, resulting from atomistic modeling the interactions of ejected hydrogen atoms from the three types of initiating radicals in the three tacticities of amorphous PP ( $\rho = 0.90 \times 10^3 \text{ kg m}^{-3}$ ), are given in Figure 2. They all peak between 4 and 5 Å and then decay exponentially to zero at around 15 to 16 Å. The corresponding mean radical-pair distances ( $\overline{r_{i,p}}$ ), are given in Tables 8–10. The values in these tables are not greatly different for the three tacticities and in all cases c-type initiating radicals give the largest mean radical-pair distances. The inter-

**Table 9. Mean Radical-Pair Distances in Amorphous PP (Head to Tail,  $\rho = 0.90 \times 10^3 \text{ kg m}^{-3}$ ):<sup>a</sup> s-PP**

initiating radicals	$\overline{r_{i,p}}/\text{\AA}$
a-type radicals	6.2367
b-type radicals	6.2017
c-type radicals	6.4373
mean	6.2919

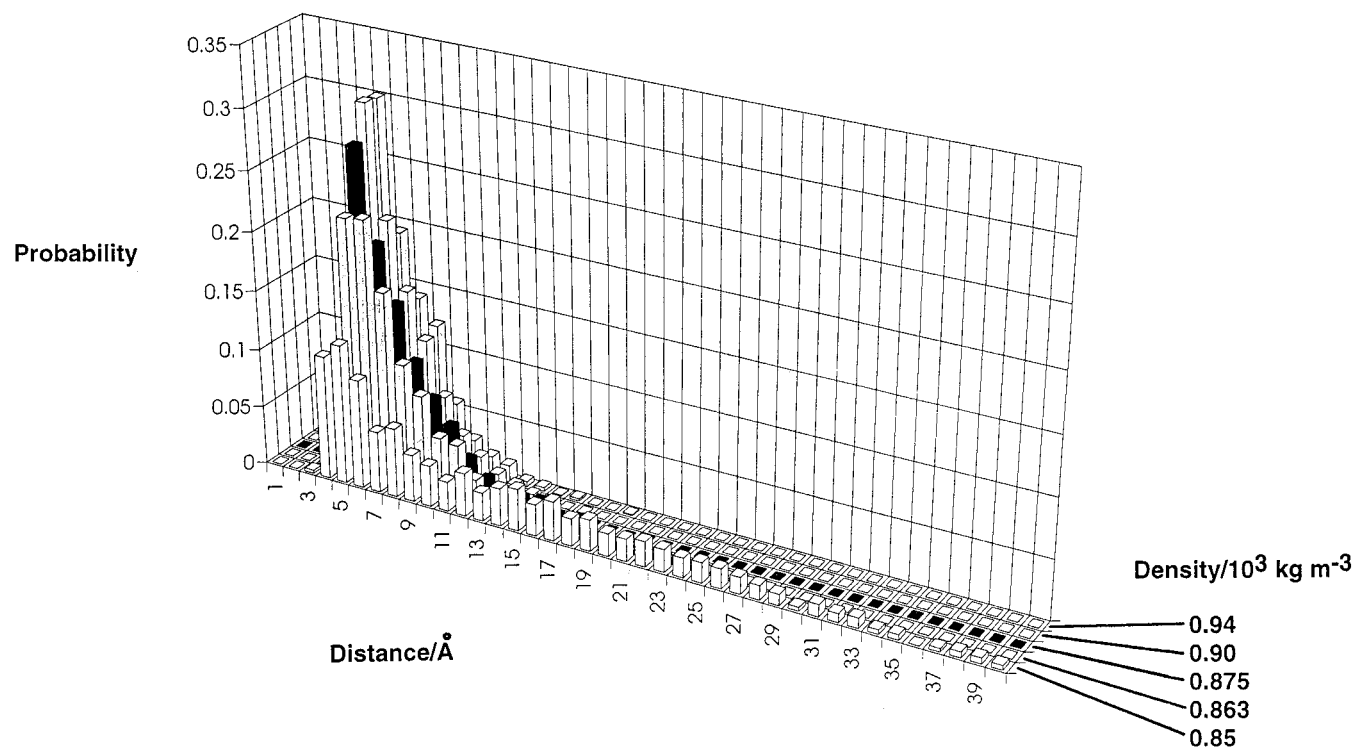
<sup>a</sup> Mean  $\equiv$  completely random a-, b-, c-type radical initiation.**Table 10. Mean Radical-Pair Distances in Amorphous PP (Head to Tail,  $\rho = 0.90 \times 10^3 \text{ kg m}^{-3}$ ):<sup>a</sup> a-PP**

initiating radicals	$\overline{r_{i,p}}/\text{\AA}$
a-type radicals	6.1586
b-type radicals	6.2642
c-type radicals	6.4350
mean	6.2859

<sup>a</sup> Mean  $\equiv$  completely random a-, b-, c-type radical initiation.**Figure 3.** MSI<sup>11</sup> interchain carbon–carbon correlation functions for the amorphous i-, s-, and a-PP cells ( $\rho = 0.90 \times 10^3 \text{ kg m}^{-3}$ ) used in this study, together with mean radical-pair distances ( $\overline{r_{i,p}}$ ).

chain carbon–carbon correlation functions (Figure 3) show probabilities for the interchain carbon–carbon distances ( $g(r)$ ), as given by MSI software,<sup>11</sup> from all pairs of carbon atoms on adjacent chains. It can be seen that the  $g(r)$  values at the mean radical-pair distances, taken over all types of initiating radicals, are 0.722, 0.656, and 0.621 for i-PP, s-PP, and a-PP, respectively. Hence, as was found for HDPE previously,<sup>1</sup> the mean radical-pair distances are only a little greater than the mean interchain distances, and most of the partner radicals are formed on immediately adjacent chains, because the ejected hydrogen atoms or protons get little

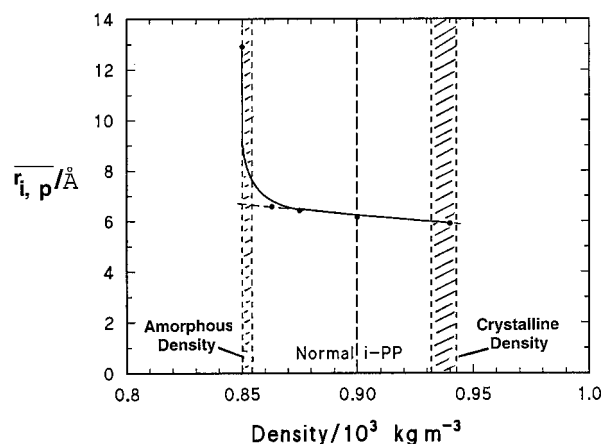




**Figure 4.** Atomistic radical-pair distance probability distribution functions for amorphous i-PPs of varying density ( $\rho = (0.85-0.94) \times 10^3 \text{ kg m}^{-3}$ ), generated by b-type initiating radicals.

chance to travel much further. For generation of partner radicals from b-type initiating radicals, which has been demonstrated to occur in reality, the mean radical-pair distances increase a little in the order i-PP < s-PP < a-PP.

**3. Effect of Density Variation on Mean Radical-Pair Distances.** Having established that only b-type initiating radicals produce sufficient b-type combined radicals to generate the ESR spectra observed experimentally by other authors, it was decided to examine the effect of density variation in i-PP on mean radical-pair distances. Macrocells were built of different densities from  $0.85 \times 10^3$  to  $0.94 \times 10^3 \text{ kg m}^{-3}$ , and the radical-pair probability-distance distribution functions, simulated by b-type initiating radicals, were generated (Figure 4). This density range was chosen because completely amorphous PP is believed to have a density of  $(0.85-0.854) \times 10^3 \text{ kg m}^{-3}$ , while completely crystalline PP has a density of  $(0.932-0.943) \times 10^3 \text{ kg m}^{-3}$ .<sup>13</sup> Although the modeling here was carried out in completely amorphous macrocells, parameters were set to yield results obtainable for polycrystalline systems. Hence, the complete range of PP densities found in normal use was covered. In Figure 4, the lowest density  $0.85 \times 10^3 \text{ kg m}^{-3}$ , has a very blunt peak at 4–5 Å and a long tailing distribution to around 40 Å. The long tail is immediately lost by  $0.863 \times 10^3 \text{ kg m}^{-3}$  where an exponential decay to zero probability at around 15–16 Å occurs. Thereafter, the peak probability becomes sharper and the curve returns to the form seen previously for the three tacticities at  $0.9 \times 10^3 \text{ kg m}^{-3}$  (Figure 2). The mean radical-pair distances, corresponding to the distribution functions shown in Figure 4, are plotted in Figure 5 as a function of density. It can be seen from Figure 5 that density variation has only a small effect on the mean radical-pair distance except in the completely amorphous density region. Since the density of completely amorphous i-PP had to be calculated from



**Figure 5.** Atomistic mean radical-pair distance ( $\overline{r_{i,p}}$ ) variation in amorphous i-PP of varying density ( $\rho = (0.85-0.94) \times 10^3 \text{ kg m}^{-3}$ ), generated from b-type initiating radicals.

liquid i-PP data,<sup>13</sup> it is hardly ever likely to be encountered in solid i-PP. s-PP and a-PP are expected to produce similar mean radical-pair distance versus density variation profiles over the same range of densities.

## Conclusions

b-Type partners have the lowest probability of being formed in all three PPs, because there is only one H atom available on the b carbon. The atomistic ratio of partner probabilities deviated only a little from the numerical availability of hydrogen atoms on the respective a-, b-, and c-type carbons of the three tacticities of PP. The deviations resulted from geometrical screening effects. Since b-type partners have the lowest probability of being formed, nearly all the initiating radicals must be b-type, in order to produce the combined radical ESR spectra observed experimentally.<sup>6,8</sup> This is in keeping with the theory of exciton energy transfer in PP,<sup>12</sup> which

demonstrates that the hydrogen on the b carbon is most easily ejected or transferred, and scission of the methyl side group is not expected.

The atomistic radical-pair distance distribution functions, resulting from all types of radical initiation in the three tacticities of amorphous PP ( $\rho = 0.90 \times 10^3 \text{ kg m}^{-3}$ ), all peak between 4 and 5 Å and then decay exponentially to zero at around 15–16 Å. Most of the partner radicals are formed on immediately adjacent chains, because the ejected hydrogen atoms, or proton transfers, get little chance to travel much further. This is in keeping with the results obtained from PE.<sup>1</sup> The mean radical-pair distances ( $\overline{r_{i,p}}$ ) are not greatly different for the three tacticities, being 6.15, 6.20, and 6.26 Å for b-type radical initiation in i-PP, s-PP, and a-PP, respectively. The effectiveness of radiation-induced cross-linking observed in polyalkanes, particularly in the presence of gaseous bridging agents such as acetylene, is predominantly a consequence of the close proximity of radical pairs on adjacent chains.<sup>2</sup> Density variation had only a small effect on the mean radical-pair distance in i-PP, except when completely amorphous which is never found in the solid state. Similarly, only small mean radical-pair distance variations are expected in s-PP and a-PP, over the range of densities normally encountered in the solid state.

**Acknowledgment.** The Authors thank EPSRC for funding this work as part of the "Polymer Network Materials—Computer Modeling and Linked Experimental Studies" research project (EPSRC grant number: GR/L62306).

## References and Notes

- (1) Jones, R. A.; Taylor, D. J. R.; Stepto, R. F. T.; Ward, I. M. Computer Modelling of the Formation of Radical Pairs in

Amorphous High Density Polyethylene (HDPE). *J. Polym. Sci., B: Polym. Phys.* **1996**, *34*, 901–908.

- (2) Jones, R. A.; Ward, I. M.; Taylor, D. J. R.; Stepto, R. F. T. Reactions of amorphous PE radical-pairs *in-vacuo* and in acetylene: a comparison of gel fraction data with Flory-Stockmayer and atomistic modelling analyses. *Polymer* **1997**, *37* (16), 3643–3657.
- (3) Jones, R. A.; Groves, D. J.; Ward, I. M. An Investigation into the Relationship between "Gel-effective" and Total Numbers of Cross-links in Irradiated LLDPE. *Polymer Int.* **1997**, *44*, 300–310.
- (4) Jones, R. A.; Groves, D. J.; Ward, I. M.; Taylor, D. J. R.; Stepto, R. F. T. Gel Fractions and Chain Reactions in Irradiated Polyethylenes. *Nuclear Inst. Methods Phys. Res., B* **1999**, *151*, 213–217. (Also in: *Ionizing Radiation and Polymers*; Proc. 3rd. Int. Symp. Ionizing Radiation and Polymers (IRaP '98), Knolle, W., Trautmann, C., Eds.; North-Holland: The Netherlands, 1999; pp 213–217.)
- (5) Dubinskii, A. A.; Grinberg, O. Ya.; Tabachnik, A. A.; Lebedev, Ya. S. Radical Pairs in the Radiolysis of Solid Paraffines: Mechanism of Radiolytic Initiation and Post Irradiation Decay. *High Energy Chem.* **1977**, *11* (2), 125–129.
- (6) Iwasaki, M.; Ichikawa, T.; Ohmori, T. Pairwise Trapping of Radicals in Irradiated High Polymers as Studied by Electron Spin Resonance. *J. Chem. Phys.* **1969**, *50* (5), 1984–90.
- (7) Iwasaki, M.; Ichikawa, T.; Ohmori, T. Pairwise Trapping of Radicals in Irradiated n-Hydrocarbons and Related Compounds as Studied by Electron Spin Resonance. *J. Chem. Phys.* **1969**, *50* (5), 1991–97.
- (8) Ooi, T.; Shiotsubo, M.; Shinohara, K. ESR Study of  $\gamma$ -Irradiated Isotactic and Atactic Polypropylene. *Polymer* **1975**, *16*, 510–515.
- (9) Demeyer, A.; Ceulemans, J. *J. Phys. Chem. A* **1997**, *101*, 3537.
- (10) Demeyer, A.; Steinlet, D.; Ceulemans, J. *J. Phys. Chem.* **1994**, *98*, 5830.
- (11) MSI, 9685 Scranton Road, San Diego, CA 92121-277.
- (12) Partridge, R. Excitation Energy Transfer in Alkanes. I. Exciton Model. II. Experimental Demonstration. III. Radiation Chemistry of Alkane Polymers. *J. Chem. Phys.* **1970**, *52* (5) 2485–2510.
- (13) *Polymer Handbook*, 2nd. ed.; Brandrup, J., Immergut, E. H., Eds.; Wiley: London, 1975; pp V-23.

MA9906229